

Package ‘randPedPCA’

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Type Package

Title Fast PCA for Large Pedigrees

Version 1.0.0

Description Compute PCAs of large pedigrees such as found in breeding populations! This package, 'randPedPCA', exploits sparse matrices and randomised linear algebra to deliver a gazillion-times speed-up compared to naive SVD (and eigen decomposition).

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dspc	<i>Add downsampling index to rppca object</i>
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Description

This index is used by plot.rppca to downsample the col (colour) values. It is stored in the rppca object's ds slot.

Usage

```
dspc(pc, to = 10000)
```

Arguments

- pc an object of class rppca
- to The down-sampling parameter. A numeric > 0 or a vector or NA. Interpreted as a proportion or integer or a index vector, see details.

Details

The parameter to is used to specify and possibly which individuals are sampled. If NA, all individuals are retained. If to is of length one and is between 0 and 1, then it is interpreted as a proportion. If it is greater than 1, it is taken to be the number of individuals to be sampled (possibly rounded by sample.int). If to is a logical or an integer vector, it is used for logical or integer indexing, respectively. The integer indices of the sample individuals are written to the ds slot. If ds exists, it is overwritten with a warning.

Value

An (invisible) object of class rppca with a slot ds added.

getNumVectorsHutchinson	<i>Compute the number of vectors to use for Hutchinson trace estimation</i>
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Description

Follows Skorski, M. (2021). Modern Analysis of Hutchinson’s Trace Estimator. 2021 55th Annual Conference on Information Sciences and Systems (CISS), 1–5. <https://doi.org/10.1109/CISS50987.2021.9400306>

Usage

getNumVectorsHutchinson(e, d)

Arguments

- e A numeric denoting the relative error margin
- d A numeric. 1-d is the probability the the relative error is bounded by e.

Value

a scalar

hutchpp	<i>Hutch++ trace estimation</i>
---------	---------------------------------

Description

Hutch++ trace estimation

Usage

```
hutchpp(  
  B,  
  num_queries = 10,  
  sketch_frac = 2/3,  
  center = FALSE,  
  oraculum = oraculumLi  
)
```

Arguments

- B An object related to the matrix A for which the trace is to be estimated
- num_queries Number of random vectors to draw
- sketch_frac Hutch++ detail
- center Whether or not to implicitly centre
- oraculum The oracle function to use

Details

The Hutch++ algorithm (Meyer et al. 2021, <https://doi.org/10.48550/arXiv.2010.09649>) estimates the trace of a matrix A by evaluating matrix vector products of A and (sub-gaussian) random vectors. This is used on a matrix B which is related to A through some function. The oracle function has to be chosen so that oracle(B, G) returns the product A the oracle function is set to work on a pedigree's L inverse matrix. But this implementation is general and should work - given a custom oracle function - on other input too.

In the context of pedigree PCA, this is used to estimate the trace of an (implicitly) centred additive relationship matrix.

There logical parameter center allows for a pedigree's L matrix to be (implicitly) centred. This is important because centring changes the total variance of the data and thus the trace of A.

Value

An estimate of A's trace - numeric

Examples

```
hutchpp(pedLInv)
hutchpp(pedLInv, center=TRUE)
```

importLinv

Generate spam object from L inverse file

Description

RandPedPCA relies in the spam onject format. But matrices are commonly stored in other formats.

Usage

```
importLinv(pth)
```

Arguments

pth path to matrix market file for L inverse matrix in dgTMatrix format

Value

A spam sparse matrix

`pedLInv`*Example pedigree L inverse matrix*

Description

An L inverse matrix generated from an AlphaSimR simulation of 20 generations. An original population splits into sub-populations A and B. After a number of generations, crossbreeding starts.

Usage`pedLInv`**Format**

'pedLInv' Matrix object of class 'spam' of dimension 2650x2650, with 7750 (row-wise) nonzero elements. Density of the matrix is 0.11 Class 'spam' (32-bit)

Source

Simulation

`pedLInv2`*Example pedigree L inverse matrix*

Description

An L inverse matrix generated from an AlphaSimR simulation of 20 generations. Two diverged populations A and B. After a number of generations, crossbreeding starts.

Usage`pedLInv2`**Format**

'pedLInv2' Matrix object of class 'spam' of dimension 2650x2650, with 7750 (row-wise) nonzero elements. Density of the matrix is 0.11 Class 'spam' (32-bit)

Source

Simulation

pedLInv4

Example pedigree L inverse matrix

Description

An L inverse matrix generated from an AlphaSimR simulation of 20 generations. One population, ABCD, is split into four, A, B, C, D.

Usage

```
pedLInv4
```

Format

```
## 'pedLInv4' Matrix object of class 'spam' of dimension 4200x4200, with 12200 (row-wise)
nonzero elements. Density of the matrix is 0.0692 Class 'spam' (32-bit)
```

Source

Simulation

pedMeta

Metadata associated with the example pedigree

Description

A dataframe.

Usage

```
pedMeta
```

Format

```
## 'pedMeta' A 'data.frame' of 2650 individuals (rows) with 12 variables (cols):
```

id Integer individual ID

population Population code. A, B or AB

generation Generation of the individual

mid dam ID

fid sire ID

gv1 genetic value

pv1 phenotypic value

gv2 genetic value

pv2 phenotypic value
gv genetic value
pv phenotypic value
generationPlotShift for plotting

Source

Simulation

```
pedMeta2      #' Example genotype data #' #' An genotype matrix (0/1/2) gener-
               ated from an AlphaSimR simulation of 20 generations. #' An original
               population splits into sub-populations A and B. After a number of #'
               generations, crossbreeding starts. #' #' #' @format ## 'pedGeno'
               #' Matrix of 2650 rows (inidividuals) and 11000 columns (SNPs) #'
               @source Simulation "pedGeno" Metadata associated with the 2nd ex-
               ample pedigree
```

Description

A dataframe.

Usage

```
pedMeta2
```

Format

'pedMeta2' A 'data.frame' of 2650 individuals (rows) with 12 variables (cols):

id Integer individual ID
population Population code. A, B or AB
generation Generation of the individual
mid dam ID
fid sire ID
gv1 genetic value
pv1 phenotypic value
gv2 genetic value
pv2 phenotypic value
gv genetic value
pv phenotypic value
generationPlotShift for plotting

Source

Simulation

```
pedMeta4      #' Example genotype data 2 #' #' An genotype matrix (0/1/2) generated from an AlphaSimR simulation of 20 generations. #' Two diverged populations A and B. After a number of #' generations, cross-breeding starts. #' #' #' @format ## 'pedGeno2' #' Matrix of 2650 rows (inidividuals) and 11000 columns (SNPs) #' @source Simulation "pedGeno2" Metadata associated with the 2nd example pedigree
```

Description

A dataframe.

Usage

```
pedMeta4
```

Format

'pedMeta4' A 'data.frame' of 4200 individuals (rows) with 9 variables (cols):

id Integer individual ID

population Population code. A, B, C, D, or ABCD

generation Generation of the individual

mid dam ID

fid sire ID

gv1 genetic value

pv1 phenotypic value

gv2 genetic value

pv2 phenotypic value

Source

Simulation

plot3D	<i>3D plot using rgl</i>
--------	--------------------------

Description

A simple wrapper around rgl's pot3d function.

Usage

```
plot3D(x, dims = c(1, 2, 3), xlab = NULL, ylab = NULL, zlab = NULL, ...)
```

Arguments

x	an rppca object
dims	vector of length 3 - indices of the PCs to plot
xlab	(optional) x axis label
ylab	(optional) yaxis label
zlab	(optional) xz axis label
...	additional arguments passed to rgl::plot3d

Details

Note, different to `plot.rppca`, which is relatively slow, `plot3D` does not down-sample the principal components and it ignores the `ds` slot of an `rppca` object if present.

Value

No return value, called for its side effects.

Examples

```
pc <- rppca(pedLInv)
plot3D(pc)

ped <- pedigree(sire=pedMeta$fid, dam=pedMeta$mid, label=pedMeta$id)
pc2 <- rppca(ped)
plot3D(pc2)
```

plot3DWithProj	<i>3D plot of PC scores with projections on coordinate planes</i>
----------------	---

Description

3D plot of PC scores with projections on coordinate planes

Usage

```
plot3DWithProj(
  pc,
  dims = c(1, 2, 3),
  plotProj = TRUE,
  grid = TRUE,
  col = 1,
  ff = 0.5,
  theta = -45,
  phi = 25
)
```

Arguments

pc	An rppca object
dims	integer vector, which PCs to plot, defaults to 1:3
plotProj	logical, whether to plot the projections
grid	logical, wheter to plot grids
col	the dot colours, integer or string, scalar or vector
ff	numeric, offset for projection (proportion of the orthogonal axis's range)
theta, phi	polar coordinates in degrees. theta rotates round the vertical axis. phi rotates round the horizontal axis.

Value

nothing

Examples

```
ped <- pedigree(pedMeta$fid,
  pedMeta$mid,
  pedMeta$id
)
pc <- rppca(ped)
plot3DWithProj(pc, col=as.numeric(factor(pedMeta$population)))
```

randRangeFinder	<i>Generate range matrix for SVD</i>
-----------------	--------------------------------------

Description

Generate range matrix for SVD

Usage

```
randRangeFinder(L, rank, depth, numVectors, cent = FALSE)
```

Arguments

L	a pedigree's L inverse matrix in sparse 'spam' format
rank	An integer, how many principal components to return
depth	integer, number of iterations for generating the range matrix
numVectors	An integer > rank, to specify the oversampling for the
cent	logical whether or not to (implicitly) 'centre' the additive relationship matrix, or more precisely, its underlying 'data matrix' L

Value

The range matrix for randSVD

randSVD	<i>Singular value decomposition in sparse triangular matrix</i>
---------	---

Description

Uses randomised linear algebra, see Halko et al. (2010). Singular value decomposition (SVD) decomposes a matrix $X = U\Sigma W^T$

Usage

```
randSVD(L, rank, depth, numVectors, cent = FALSE)
```

Arguments

L	a pedigree's L inverse matrix in sparse 'spam' format
rank	An integer, how many principal components to return
depth	integer, the number of iterations for generating the range matrix
numVectors	An integer > rank to specify the oversampling for the
cent	logical, whether or not to (implicitly) centre the additive relationship matrix

Value

A list of three: u ($=U$), d ($=\text{Sigma}$), and v ($=W^T$)

randTraceHutchinson	<i>Trace estimation for sparse L inverse matrices</i>
---------------------	--

Description

Using Hutchinson's method

Usage

```
randTraceHutchinson(L, numVectors)
```

Arguments

L	A pedigree's L inverse matrix
numVectors	an integer specifying how many random vectors to use If you do not have a good reason to do otherwise, use the function <code>hutchpp</code> instead. The higher numVectors, the higher the accuracy and the longer the running time. Accuracy can be estimated with the function <code>getNumVectorsHutchinson</code> .

Value

a scalar

rppca	<i>Fast pedigree PCA using sparse matrices and randomised linear algebra</i>
-------	--

Description

Fast pedigree PCA using sparse matrices and randomised linear algebra

Usage

```
rppca(X, ...)  
  
## S3 method for class 'spam'  
rppca(  
  X,  
  method = "randSVD",  
  rank = 10,  
  depth = 3,
```

```

    numVectors = 15,
    totVar = NULL,
    center = FALSE,
    ...
)

## S3 method for class 'pedigree'
rppca(
  X,
  method = "randSVD",
  rank = 10,
  depth = 3,
  numVectors = 15,
  totVar = NULL,
  center = FALSE,
  ...
)
```

Arguments

<code>X</code>	A representation of a pedigree, see Details.
<code>...</code>	optional arguments passed to methods
<code>method</code>	string only randSVD (the default) is implemented
<code>rank</code>	integer how many principal components to return
<code>depth</code>	integer number of iterations for generating the range matrix
<code>numVectors</code>	integer > rank to specify the oversampling for the range matrix
<code>totVar</code>	scalar (optional) the total variance, required for computation of variance proportions when using an L-inverse matrix as input
<code>center</code>	logical whether or not to (implicitly) centre the additive relationship matrix

Details

The output slots are named like those of R's built in `prcomp` function. Rotation is not returned by default as it is the transpose of the PC scores, which are returned in `x`. `scale` and `center` are set to `FALSE`.

Value

A list containing:

- `x` the principal components
- `sdev` the variance components of each PC. Note that the total variance is not known per se and this these components cannot be used to compute the proportion of the total variance accounted for by each PC. However, if `nVecTraceEst` is specified, `rppca` will estimate the total variance and return variance proportions.
- `vProp` the estimated variance proportions accounted for by each PC. Only returned if `totVar` is set.

scale always FALSE
 center logical indicating whether or not the implicit data matrix was centred
 rotation the right singular values of the relationship matrix. Only returned if returnRotation == TRUE
 varProps proportion of the total variance explained by each PC. Only returned if starting from a pedigree object without centring, or if totVar is supplied.

Examples

```

pc <- rppca(pedLInv)
ped <- pedigree(sire=pedMeta$fid,
               dam=pedMeta$mid,
               label=pedMeta$id
             )
pc2 <- rppca(ped)

```

sparse2spam	<i>Convert generic sparse matrix to spam format</i>
-------------	---

Description

Convert generic sparse matrix to spam format

Usage

```
sparse2spam(sprs)
```

Arguments

sprs A sparse matrix.

Value

A spam sparse matrix

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