Package 'profileCI'

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Title Profiling a Log-Likelihood to Calculate Confidence Intervals

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Description Provides tools for profiling a user-supplied log-likelihood function to calculate confidence intervals for model parameters. Speed of computation can be improved by adjusting the step sizes in the profiling and/or starting the profiling from limits based on the approximate large sample normal distribution for the maximum likelihood estimator of a parameter. The accuracy of the limits can be set by the user. A plot method visualises the log-likelihood and confidence interval. Only convex log-likelihoods are supported, that is, disjoint confidence intervals will not be found.

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profileCI-package profileCI: Profiling a Log-Likelihood to Calculate Confidence Intervals

Description

Provides tools for profiling a user-supplied log-likelihood function to calculate confidence intervals for model parameters. Speed of computation can be improved by adjusting the step sizes in the profiling and/or starting the profiling from limits based on the approximate large sample normal distribution for the maximum likelihood estimator of a parameter. The accuracy of the limits can be set by the user. A plot method visualises the log-likelihood and confidence interval. Only convex log-likelihoods are supported, that is, disjoint confidence intervals will not be found.

Details

The main function is profileCI, which profiles the log-likelihood, with respect to one parameter at a time.

Author(s)

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See Also

profileCI and plot.profileCI.

logLikFn

Calculate Log-Likelihood

Description

This is a generic function for calculating a log-likelihood for an object at input parameter values.

Usage

```
logLikFn(object, pars, ...)
## S3 method for class 'glm'
logLikFn(object, pars, ...)
```

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Arguments

object	A fitted model object.
pars	A numeric vector of parameters of the model.
	Further arguments.

Details

This generic function has been created to enable a function that calculates the log-likelihood for a parametric model at a given set of parameter values in pars to be available to the function profileCI.

Value

A numeric scalar. The value of the log-likelihood function for the fitted model object object for parameter values pars.

profileCI

Confidence Intervals using Profile Likelihood

Description

Calculates confidence intervals for one or more parameters in a fitted model object. A function that returns the log-likelihood must be supplied, either directly via the argument loglik or using a logLikFn S3 generic.

Usage

```
profileCI(
   object,
   loglik,
   ...,
   parm = "all",
   level = 0.95,
   profile = TRUE,
   mult = 32,
   faster = TRUE,
   epsilon = -1,
   optim_args = list()
)
```

Arguments

object

A fitted model object. This object must have a coef S3 method. If faster = TRUE then it must also have a vcov S3 method.

loglik	A named function that returns the log-likelihood based on input parameter values and data. The first argument must be the vector of model parameters. If the likelihood is zero for any observation in the data then the function should return -Inf.
	Alternatively, loglik does not need to be supplied if a logLikFn S3 method has been created for object. The profileCI package provides logLikFn.glm, which is used in an example in Examples .
	Further arguments to be passed to loglik.
parm	A vector specifying the parameters for which confidence intervals are calculated, either a vector of numbers or a vector of names. The default, which = "all", produces confidence intervals for all the parameters.
level	The confidence level required. A numeric scalar in $(0, 1)$.
profile	A logical scalar. If TRUE then confidence intervals based on a profile log-likelihood are returned. If FALSE then intervals based on approximate large sample normal theory, which are symmetric about the MLE, are returned.
mult	A positive numeric scalar. Controls the increment by which the parameter of interest is increased/decreased when profiling above/below its MLE. The increment is $mult * se / 100$ where se is the estimated standard error of the estimator of the parameter. Decreasing mult profiles at more points but will be slower.
faster	A logical scalar. If faster = TRUE then the profiling of the log-likelihood is in search of a lower (upper) confidence limit is started at the corresponding symmetric lower (upper) confidence limit.
epsilon	Only relevant if profile = TRUE. A numeric vector of values that determine the accuracy of the confidence limits. epsilon is recycled to the length of the parameter vector parm.
	 If epsilon[i] > 0 then this value is passed as the argument epsilon to the itp::itp function, which estimates the parameter values for which the profile log-likelihood for parameter i drops to the value that defines the confidence limits, once profiling has been successful in finding an interval within which this value lies.
	• If epsilon[i] < 0 quadratic interpolation is used, which will tend to be faster.
	• If epsilon[i] = 0 then linear interpolation is used, which will be faster still.
optim_args	A list of further arguments (other than par and fn) to pass to [stats::optim].

Details

The default, epsilon = -1, should work well enough in most circumstances, but to achieve a specific accuracy set epsilon to be a small positive value, for example, epsilon = 1e-4.

The defaults mult = 32 and faster = TRUE are designed to calculate confidence intervals fairly quickly. If the object returned from profileCI is plotted, using plot.profileCI, then we will not obtain a smooth plot of a profile log-likelihood. Setting faster = FALSE and reducing mult, perhaps to 8 or 16 should produce a smoother plot.

profileCI

Value

An object of class c("profileCI", "matrix", "array"). A numeric matrix with 2 columns giving the lower and upper confidence limits for each parameter. These columns are labelled as (1-level)/2 and 1-(1-level)/2, expressed as a percentage, by default 2.5% and 97.5%. The row names are the names of the parameters supplied in parm.

If profile = TRUE then the returned object has extra attributes crit, level and for_plot. The latter is a named list of length equal to the number of parameters. Each component is a 2-column numeric matrix. The first column contains values of the parameter and the second column the corresponding values of the profile log-likelihood. The profile log-likelihood is equal to the attribute crit at the limits of the confidence interval. The attribute level is the input argument level. If faster = FALSE or epsilon > 0 then the attributes lower_pars and upper_pars are lists that provide, for each profiling, the values of the parameters for the last maximisation of the log-likelihood.

A matrix with columns giving the object c("profileCI", "matrix", "array").

See Also

plot.profileCI and print.profileCI.

Examples

```
## From example(glm)
counts <- c(18, 17, 15, 20, 10, 20, 25, 13, 12)
outcome <- gl(3, 1, 9)
treatment <- gl(3, 3)
glm.D93 <- glm(counts ~ outcome + treatment, family = poisson())</pre>
confint(glm.D93)
confint.default(glm.D93)
# A logLikFn.glm S3 method is provided in profileCI so we do not need to
# supply loglik explicitly
prof <- profileCI(glm.D93)</pre>
prof
# Supplying a Poisson GLM log-likelihood explicitly
poisson_loglik <- function(pars) {</pre>
 lambda <- exp(model.matrix(glm.D93) %*% pars)</pre>
 loglik <- stats::dpois(x = glm.D93$y, lambda = lambda, log = TRUE)</pre>
 return(sum(loglik))
}
# This will be a bit slower than profile.glm() because glm.fit() is fast
prof <- profileCI(glm.D93, loglik = poisson_loglik)</pre>
prof
plot(prof, parm = 1)
plot(prof, parm = "outcome2")
# Supplying a more general Poisson GLM log-likelihood
poisson_loglik_2 <- function(pars, glm_object) {</pre>
 lambda <- exp(model.matrix(glm_object) %*% pars)</pre>
 loglik <- stats::dpois(x = glm_object$y, lambda = lambda, log = TRUE)</pre>
 return(sum(loglik))
```

```
} prof <- profileCI(glm.D93, loglik = poisson_loglik_2, glm_object = glm.D93)
prof</pre>
```

profileCI_methods Methods for objects of class "profileCI"

Description

Methods for objects of class "profileCI" returned from profileCI.

Usage

```
## S3 method for class 'profileCI'
print(x, ...)
## S3 method for class 'profileCI'
```

plot(x, parm = 1:nrow(x), add = TRUE, digits = 2, ...)

Arguments

x	An object inheriting from class profileCI", a result of a call to profileCI.
	Further arguments. For print. "profileCI" to pass arguments to print. For plot.profileCI to pass graphical parameters to graphics::plot to create the initial plot of the profile log-likelihood.
parm	A numeric or character scalar specifying the parameter for which a profile log- likelihood is plotted. Must be a single component consistent with the argument parm to profileCI.
add	A logical scalar. If add = TRUE then the plot is annotated with a horizontal line indicating the critical value for the profile log-likelihood used to calculate the confidence limits, vertical lines indicating the values of these limits and a legend stating the confidence interval.
digits	An integer. Passed to signif to round the confidence limits in the legend, if add = TRUE.

Details

print.profileCI. A numeric matrix with 2 columns giving the lower and upper confidence limits for the parameters specified by the argument parm in profileCI. These columns are labelled as (1-level)/2 and 1-(1-level)/2, expressed as a percentage, by default 2.5% and 97.5%.

plot.profileCI. A plot is produced of the profile log-likelihood for the parameter chosen by parm. Only the parameter values used to profile the log-likelihood in the call to profileCI are included, so if faster = TRUE was used then the plot will not be of a smooth curve but will be triangular in the middle.

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Value

print.profileCI: the argument x is returned, invisibly.

plot.profileCI: a numeric vector containing the confidence interval for the parameter chosen for the plot.

Examples

See profileCI.

See Also

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