# Package 'conTree'

November 22, 2023

Type Package

Title Contrast Trees and Boosting

Description Contrast trees represent a new approach for assessing the accuracy of many types of machine learning estimates that are not amenable to standard (cross) validation methods; see ``Contrast trees and distribution boosting", Jerome H. Friedman (2020) <doi:10.1073/pnas.1921562117>. In situations where inaccuracies are detected, boosted contrast trees can often improve performance. Functions are provided to to build such trees in addition to a special case, distribution boosting, an assumption free method for estimating the full probability distribution of an outcome variable given any set of joint input predictor variable values.

Version 0.3-1

VignetteBuilder knitr

**License** Apache License 2.0

**Encoding UTF-8** 

URL https://jhfhub.github.io/conTree\_tutorial/

BugReports https://github.com/bnaras/conTree/issues

Imports stats, graphics RoxygenNote 7.2.3

Suggests randomForest, knitr, rmarkdown

LazyData true

**Depends** R (>= 3.5)

**NeedsCompilation** yes

Author Jerome Friedman [aut, cph],

Balasubramanian Narasimhan [aut, cre]

Maintainer Balasubramanian Narasimhan <naras@stanford.edu>

Repository CRAN

**Date/Publication** 2023-11-22 09:20:12 UTC

2 conTree-package

# **R** topics documented:

conTree-package	2
age_data	3
air_quality	3
census	4
contrast	5
getnodes	10
lofcurve	11
nodesum	12
onesample_parameters	13
predtrast	14
prune	15
prune.seq	15
save_rfun	16
treesum	16
xval	17
ydist	18
	19
	19

conTree-package

Contrast and Boosted Trees

# Description

Index

Contrast trees represent a new approach for assessing the accuracy of many types of machine learning estimates that are not amenable to standard (cross) validation methods. In situations where inaccuracies are detected, boosted contrast trees can often improve performance. Functions are provided to to build such trees in addition to a special case, distribution boosting, an assumption free method for estimating the full probability distribution of an outcome variable given any set of joint input predictor variable values.

# Author(s)

Original code (C) by Jerome H. Friedman, minor modifications, formatting, and packaging by Balasubramanian Narasimhan

#### References

Jerome Friedman (2019). *Contrast Trees and Distribution Boosting* https://arxiv.org/abs/1912.03785

age\_data 3

age\_data

Age and Demographics data

### **Description**

The data come from 9243 questionnaires filled out by shopping mall customers in the San Francisco Bay Area (Impact Resources, Inc., Columbus, OH). Here we attempt to estimate a persons age as a function of the other 13 demographic variables. For this data set age value is reported as being in one of seven intervals {13–17, 18–24, 25–34, 35–44, 45–54, 55–64, >= 65}. Each persons age is randomly generated uniformly within its corresponding reported interval. For the last interval an exponential distribution was used with mean corresponding to life expectancy after reaching age 65.

# Usage

age\_data

#### **Format**

age\_data:

A list of 3 items.

xage data frame of 8856 observations on 13 variables

yage Randomly generated age in the range above

**gbage** gradient boosting model for median age given x

# Source

The Elements of Statistical Learning, Data Mining, Second Edition, by Hastie, Tibshirani, and Friedman.

air\_quality

Air Quality Data from UC Irvine Machine Learning Repository

#### **Description**

The data set consists of hourly averaged measurements from an array of 5 metal oxide chemical sensors embedded in an air quality chemical multisensor device. The outcome variable y is the corresponding true hourly averaged concentration CO taken from a reference analyzer. The input variables x are taken to be the corresponding hourly averaged measurements of the 13 other quantities.

### Usage

air\_quality

4 census

#### **Format**

```
air_quality:
A list with 4 items.

xco data frame of 9357 observations on 13 variables
yco hourly averaged CO concentration
zco sample membership indicator
pr2 probability propensity score
```

#### Source

https://archive.ics.uci.edu/ml/datasets/air+quality

census

Census Data Example from UC Irvine Machine Learning Repository

# Description

Includes a data frame of 1994 US census income from 48,842 people divided into a training set of 32,561 and an independent test set of 16,281. The training outcome variable y (yt for test) is binary and indicates whether or not a person's income is greater than \$50,000 per year. There are 12 predictor variables x (xt for test) consisting of various demographic and financial properties associated with each person. It also included estimates of Pr(y=1|x) obtained by several machine learning methods: gradient boosting on logistic scale using maximum likelihood (GBL), random forest (RF), and gradient boosting on the probability scale (GBP) using least–squares.

#### Usage

census

# Format

census:

A list of 10 items.

- x training data frame of 32561 observations on 12 predictor variables
- y training binary response whether salary is above \$50K or not
- xt test data frame of 16281 observations predictor variables
- yt test binary response whether salary is above \$50K or not

gbl training GBL response variable

gblt test GBL response variable

gbp training GBP response variable

gbpt test GBP response variable

rf training RF response probabilities

rft test GBP response probabilities

# Source

https://archive.ics.uci.edu/ml/datasets/census+income

contrast

Build contrast tree

# **Description**

Build contrast tree

Build boosted contrast tree model

Bootstrap contrast trees

# Usage

```
contrast(
 х,
 у,
 z,
 w = rep(1, nrow(x)),
 cat.vars = NULL,
  not.used = NULL,
  qint = 10,
  xmiss = 9e+35,
  tree.size = 10,
 min.node = 500,
 mode = c("onesamp", "twosamp"),
  type = "dist",
  pwr = 2,
  quant = 0.5,
  nclass = NULL,
  costs = NULL,
  cdfsamp = 500,
  verbose = FALSE,
  tree.store = 1e+06,
  cat.store = 1e+05,
  nbump = 1,
  fnodes = 0.25,
  fsamp = 1,
  doprint = FALSE
)
modtrast(
 Х,
 у,
  z,
 w = rep(1, nrow(x)),
```

```
cat.vars = NULL,
 not.used = NULL,
 qint = 10,
 xmiss = 9e+35,
  tree.size = 10,
 min.node = 500,
  learn.rate = 0.1,
  type = c("dist", "diff", "class", "quant", "prob", "maxmean", "diffmean"),
  pwr = 2,
  quant = 0.5,
  cdfsamp = 500,
  verbose = FALSE,
  tree.store = 1e+06,
  cat.store = 1e+05,
  nbump = 1,
  fnodes = 0.25,
  fsamp = 1,
  doprint = FALSE,
 niter = 100,
 doplot = FALSE,
  span = 0,
 plot.span = 0.15,
 print.itr = 10
bootcri(
 х,
 у,
 w = rep(1, nrow(x)),
 cat.vars = NULL,
 not.used = NULL,
 qint = 10,
 xmiss = 9e+35,
  tree.size = 10,
 min.node = 500,
 mode = "onesamp",
  type = "dist",
  pwr = 2,
  quant = 0.5,
 nclass = NULL,
 costs = NULL,
  cdfsamp = 500,
  verbose = FALSE,
  tree.store = 1e+06,
  cat.store = 1e+05,
  nbump = 100,
  fnodes = 1,
```

```
fsamp = 1,
doprint = FALSE
)
```

# Arguments

rguments	
X	training input predictor data matrix or data frame. Rows are observations and columns are variables. Must be a numeric matrix or a data frame.
У	vector, or matrix containing training data input outcome values or censoring intervals for each observation. if y is a vector then it implies that y uncensored outcome values or other contrasting quantity. If y is a matrix, then then y is assumed to be censoring intervals for each observation; see details below
Z	vector containing values of a second contrasting quantity for each observation
W	training observation weights
cat.vars	vector of column labels (numbers or names) indicating categorical variables (factors). All variables not so indicated are assumed to be orderable numeric; see details below
not.used	vector of column labels (numbers or names) indicating predictor variables not to be used in the model
qint	maximum number of split evaluation points on each predictor variable
xmiss	missing value flag. Must be numeric and larger than any non missing predictor/abs(response) variable value. Predictor variable values greater than or equal to xmiss are regarded as missing. Predictor variable data values of NA are internally set to the value of xmiss and thereby regarded as missing
tree.size	maximum number of terminal nodes in generated trees
min.node	minimum number of training observations in each tree terminal node
mode	indicating one or two-sample contrast; see details below for how it works with type
type	type of contrast; see details below for how it works with mode
pwr	center split bias parameter. Larger values produce less center split bias.
quant	specified quantile p (type='quant' only)
nclass	number of classes (type ='class' only) default=2
costs	nclass by nclass misclassification cost matrix (type='class' only); default is equal valued diagonal (error rate)
cdfsamp	= maximum subsample size used to compute censored CDF (censoring only)
verbose	a logical flag indicating print/don't print censored CDF computation progress, default ${\sf FALSE}$
tree.store	size of internal tree storage. Decrease value in response to memory allocation error. Increase value for very large values of max.trees and/or tree.size, or in response to diagnostic message or erratic program behavior
cat.store	size of internal categorical value storage. Decrease value in response to memory allocation error. Increase value for very large values of max.trees and/or tree.size in the presence of many categorical variables (factors) with many levels, or in response to diagnostic message or erratic program behavior

nbump number of bootstrap replications

fnodes top fraction of node criteria used to evaluate trial bumped trees

fsamp fraction of observations used in each bootstrap sample for bumped trees

doprint logical flag TRUE/FALSE implies do/don't plot iteration progress

learn.rate learning rate parameter in (0,1]

niter number of trees

doplot a flag to display/not display graphical plots span span for qq-plot transformation smoother

plot.span running median smoother span for discrepancy plot (doplot = TRUE, only)

print.itr tree discrepancy printing iteration interval

#### **Details**

The varible xmiss is the missing value flag, Must be numeric and larger than any non missing predictor/abs(response) variable value. Predictor variable values greater than or equal to xmiss are regarded as missing. Predictor variable data values of NA are internally set to the value of xmiss and thereby regarded as missing.

If the response y is a matrix, it is assumed to contain censoring intervals for each observation. Rows are observations.

- First/second column are lower/upper boundary of censoring interval (Can be same value for uncensored observations) respectively
- y[,1] = -xmiss implies outcome less than or equal to y[,2] (censored from above)
- y[,2] = xmiss implies outcome greater than or equal to <math>y[,1]

Note that censoring is only allowed for type='dist'; see further below.

If x is a data frame and cat.vars (the columns indicating categorical variables), is missing, then components of type factor are treated as categorical variables. Ordered factors should be input as type numeric with appropriate numerical scores. If cat.vars is present it will over ride the data frame typing.

The mode argument is either

- 'onesamp' (default) meaning one x-vector for each (x,z) pair
- · 'twosamp' implies two-sample contrast with
  - x are predictor variables for both samples
  - y are outcomes for both samples
  - z is sample identity flag with z < 0 implying first sample observations and z > 0, the second sample observations. The type argument indicates the type of contrast. It can be either a user defined function or a string. If mode is 'onesamp', the default,
- type = 'dist' (default) implies contrast distribution of y with that of z (y may be censored see above)
- type = 'diff' implies contrast joint paired values of y and z
- type = 'class' implies classification: contrast class labels y[i] and z[i] are two class labels (in 1:nclass) for each observation.

• type = 'prob' implies contrast predicted with empirical probabilities: y[i] = 0/1 and z[i] is predicted probability P(y = 1) for i-th observation

- type = 'quant' is contrast predicted with empirical quantiles: y[i] is outcome value for i-th observation and z[i] is predicted p-th quantile value (see below) for i-th observation (0
- type = 'diffmean' implies maximize absolute mean difference between y and z
- type = 'maxmean' implies maximize signed mean difference between y and z

When mode is 'twosamp'

- type= 'dist' (default) implies contrast y distributions of both samples
- type = 'diffmean' implies maximize absolute difference between means of two samples
- type = 'maxmean' maximize signed difference between means of two samples

When type is a function, it must be a function of three arguments f(y,z,w) where y and z are double vectors and w is a weight vector, not necessarily normalized. The function should return a double vector of length 1 as the result. See example below.

#### Value

```
a contrast model object use as input to interpretation procedures
a contrast model object to be used with predtrast()
a named list with out$bcri the bootstraped discrepancy values
```

# Author(s)

Jerome H. Friedman

#### References

```
Jerome H. Friedman (2020). doi:10.1073/pnas.1921562117
```

#### **Examples**

```
data(census, package = "conTree")
dx <- 1:10000; dxt <- 10001:16281;
# Build contrast tree
tree <- contrast(census$xt[dx,], census$yt[dx], census$gblt[dx], type = 'prob')</pre>
# Summarize tree
treesum(tree)
# Get terminal node identifiers for regions containing observations 1 through 10
getnodes(tree, x = census$xt[1:10, ])
# Plot nodes
nodeplots(tree, x = census$xt[dx, ], y = census$yt[dx], z = census$gblt[dx])
# Summarize contrast tree against (precomputed) gradient boosting
# on logistic scale using maximum likelihood (GBL)
nodesum(tree, census$xt[dxt,], census$yt[dxt], census$gblt[dxt])
# Use a custom R discrepancy function to build a contrast tree
dfun <- function(y, z, w) {</pre>
  w <- w / sum(w)
```

10 getnodes

```
abs(sum(w * (y - z)))
}
tree2 <- contrast(census$xt[dx,], census$yt[dx], census$gblt[dx], type = dfun)
nodesum(tree2, census$xt[dxt,], census$yt[dxt], census$gblt[dxt])
# Generate lack of fit curve
lofcurve(tree, census$xt[dx,], census$yt[dx], census$gblt[dx])
# Build contrast tree boosting models
# Use small # of iterations for illustration (typically >= 200)
modgbl = modtrast(census$x, census$y, census$gbl, type = 'prob', niter = 10)
# Plot model accuracy as a function of iteration number
xval(modgbl, census$x, census$y, census$gbl, col = 'red')
# Produce predictions from modtrast() for new data.
ypred <- predtrast(modgbl, census$xt, census$gblt, num = modgbl$niter)
# Produce distribution boosting estimates
yhat <- predtrast(modgbl, census$xt, census$gblt, num = modgbl$niter)</pre>
```

getnodes

Get terminal node observation assignments

#### **Description**

Get terminal node observation assignments

#### Usage

```
getnodes(tree, x)
```

#### **Arguments**

tree model object output from contrast() or prune()

x training input predictor data matrix or data frame in same format as in contrast()

#### Value

vector of tree terminal node identifiers (numbers) corresponding to each observation (row of x)

# See Also

```
contrast()
```

lofcurve 11

lofcurve

Produce lack-of-fit curve for a contrast tree

# Description

Produce lack-of-fit curve for a contrast tree

# Usage

```
lofcurve(
   tree,
   x,
   y,
   z,
   w = rep(1, length(y)),
   doplot = "first",
   col = "black",
   ylim = NULL
)
```

# Arguments

tree	model object output from contrast() or prune()
x	training input predictor data matrix or data frame in same format as in contrast()
У	vector, or matrix containing training data input outcome values or censoring intervals for each observation in same format as in contrast()
z	vector containing values of a second contrasting quantity for each observation in same observation format as in contrast ()
W	observation weights
doplot	logical flag. doplot="first" implies start new display. doplot="next" implies super impose plot on existing display. doplot="none" implies no plot displayed.
col	color of plotted curve
ylim	y-axis limit

# Value

a named list of plotted x and y points

12 nodesum

nodesum

Summarize contrast tree

# Description

Summarize contrast tree

Show graphical terminal node summaries

# Usage

```
nodesum(tree, x, y, z, w = rep(1, nrow(x)), doplot = FALSE)

nodeplots(
    tree,
    x,
    y,
    z,
    w = rep(1, nrow(x)),
    nodes = NULL,
    xlim = NULL,
    ylim = NULL,
    pts = "FALSE",
    span = 0.15
)
```

# Arguments

tree	model object output from contrast() or prune()
x	training input predictor data matrix or data frame in same format as in contrast()
у	vector, or matrix containing training data input outcome values or censoring intervals for each observation in same format as in contrast()
Z	vector containing values of a second contrasting quantity for each observation in same observation format as in contrast()
W	observation weights
doplot	a flag to display/not display plots of output quantities
nodes	selected tree terminal node identifiers. Default is all terminal nodes
xlim	x-axis limit
ylim	y-axis limit
pts	logical flag indicating whether to show y-values as circles/points (type = 'pp' only)
span	running median smoother span (type = 'diff' only)

#### **Details**

The graphical representations of terminal node contrasts depend on the tree type graphical representations of terminal node contrasts depending on tree type -type = 'dist' implies CDFs of y and z in each terminal node. (Only top nine nodes are shown). Note that y can be censored (see above) -type = 'diff' implies plot y versus z in each terminal node. (Only top nine nodes are shown). -type = 'class' implies barplot of misclassification risk (upper) amd total weight (lower) in each terminal node -type = 'prob' implies upper barplot contrasting empirical (blue) and predicted (red) p(y=1) in each terminal node. Lower barplot showing total weight in each terminal node.

- type = 'quant' => upper barplot of fraction of y-values greater than or equal to corresponding z-values (quantile prediction) in each terminal node. Horizontal line reflects specified target quantile. Lower barplot showing total weight in each terminal node.
- type = 'diffmean' or type = 'maxmean' implies upper barplot contrasting y-mean (blue) and z-mean (red) in each terminal node. Lower barplot showing total weight in each terminal node.

#### Value

a named list of four items:

- nodes the tree terminal node identifiers
- cri the terminal node criterion values (depends on contrast type see above)
- · wt sum of weights in each terminal node
- · avecri weighted criterion average over all terminal nodes

#### See Also

contrast()

onesample\_parameters Return the one sample parameters used in fortran discrepancy functions

# **Description**

These functions are mostly useful when one wants to test one's own discrepancy function in R f(y, z, w) to determine if the results are correct. So a natural test is to experiment by programming one of the already implemented discrepancy functions in R. However, the Fortran implementations of such discrepancy measures use some parameters in the computations and therefore the returned results from a simple R implementation may not exactly match. Using these parameters, one can ensure that they do. These are to be interpreted as follows. For one sample, the type = "dist" implementation in the package returns 0 if the length of y is less than nmin which is (100L). The eps = 1.0e-5 parameter is used to ensure that the denominator in the formula for the Anderson-Darling statistic is at least eps. Next, for type = "prob", if the length of the vector is less than nmin = 20 the discrepancy is computed to be 0. And so on. Refer to the R and Fortran source for further details as this is an advanced topic.

14 predtrast

# Usage

```
onesample_parameters()
twosample_parameters()
```

#### Value

a named list for each of the types.

predtrast

Predict y-values from boosted contrast model

# Description

Predict y-values from boosted contrast model

# Usage

```
predtrast(model, x, z, num = model$niter)
```

# Arguments

model object output from modtrast()

x x-values for new dataz z-values for new data

num number of trees used to compute model values

# Value

predicted y-values for new data from model

# See Also

```
contrast()
```

prune 15

prune

Prune a contrast tree

# **Description**

Prune a contrast tree

## Usage

```
prune(tree, thr = 0.1)
```

# **Arguments**

tree a tree model object output from contrast thr a split improvement threshold, default is 0.1

#### Value

a bottom-up pruned tree with splits corresponding to improvement less than threshold thr removed

prune.seq

Show all possible pruned subtrees

# **Description**

Show all possible pruned subtrees

# Usage

```
prune.seq(tree, eps = 0.01, plot.it = TRUE)
```

# Arguments

tree a tree model object output from contrast

eps small increment defining grid of threshold values

plot.it a logical flag indicating plot/don't plot of number of nodes versus threshold

value for all pruned subtrees, default TRUE

#### Value

a named list of two items:

- thr a set of threshold values that sequentially reduce tree size
- nodes the corresponding tree sizes (number of terminal nodes)

16 treesum

save\_rfun

Save the function f for calling from fortran

# **Description**

Save the function f for calling from fortran

# Usage

```
save_rfun(f)
```

## **Arguments**

f

the R function to be called using .Fortran

### Value

TRUE, invisibly.

treesum

Print terminal node x-region boundaries

#### **Description**

Print terminal node x-region boundaries

#### Usage

```
treesum(tree, nodes = NULL)
```

# **Arguments**

tree

model object output from contrast() or prune()

nodes

vector of terminal node identifiers for the tree specifying the desired regions.

The default is all terminal nodes.

#### **Details**

The predictor variable x-boundaries defining each terminal node are printed.

For numeric variables: variable | sign | value

- sign + => value=lower boundary on variable
- sign => value upper boundary on variable

For categorical variables: cat variable | sign | set of values

- sign + => values in node
- sign => values not in node (compliment values in node) graphical representations of terminal node contrasts depend on the tree type

xval 17

# Value

No return value (invisble NULL)

# See Also

```
contrast()
```

xval

Cross-validate boosted contrast tree boosted with (new) data

# Description

Cross-validate boosted contrast tree boosted with (new) data

# Usage

```
xval(
  mdl,
  x,
  y,
  z,
  num = length(mdl$tree),
  del = 10,
  span = 0.15,
  ylab = "Average Discrepancy",
  doplot = "first",
  doprint = FALSE,
  col = "red"
)
```

# Arguments

mdl	model output from modtrast()
x	data predictor variables is same format as input to modtrast
У	data y values is same format as input to modtrast
Z	data z values is same format as input to modtrast
num	number of trees used to compute model values
del	plot discrepancy value computed every del-th iteration (tree)
span	running median smoother span (doplot=TRUE, only)
ylab	graphical parameter ('doplot="first", only)
doplot	logical flag. doplot="first" implies start new display. doplot="next" implies super impose plot on existing display. doplot="none" implies no plot displayed.
doprint	logical flag TRUE/FALSE implies do/don't print progress while executing, default FALSE
col	color of plotted curve

18 ydist

# Value

a named list of two items: ntree the iteration numbers, and error the corresponding discrepancy values

# See Also

```
contrast()
```

ydist

Transform z-values t(z) such that the distribution of p(t(z)|x) approximates p(t(y|x) for type = 'dist' only

# Description

Transform z-values t(z) such that the distribution of p(t(z)|x) approximates p(t(y|x)) for type = 'dist' only

# Usage

```
ydist(model, x, z, num = model$niter)
```

# **Arguments**

model object output from modtrast()

x vector of predictor variable values for a (single) observation

z sample of z-values drawn from p(z|x)

num number of trees used to compute model values

## Value

vector of length(z) containing transformed values  $\mathbf{t}(\mathbf{z})$  approximating p(y|x)

# See Also

```
contrast()
```

# **Index**

```
* datasets
    age_data, 3
    air_quality, 3
    census, 4
age_data, 3
air_quality, 3
bootcri (contrast), 5
census, 4
contrast, 5
contrast(), 10, 13, 14, 17, 18
getnodes, 10
lofcurve, 11
modtrast (contrast), 5
nodeplots (nodesum), 12
nodesum, 12
one sample\_parameters, 13
predtrast, 14
prune, 15
prune.seq, 15
save_rfun, 16
treesum, 16
twosample_parameters
        (onesample_parameters), 13
xval, 17
ydist, 18
```